

7.4 Biconditionals
and Good Definitions

Implications

If P then Q
Converse
If Q then P

Biconditional
(Two conditions)

if then to if and only if
(iff)

Implication

If it is sunny then I open the window

Converse

If I open the window then it is sunny

Biconditional

It is sunny iff I open the window

P
The sum of two integers is even
iff the two integers are even
 Q

F If the sum of two integers is even
then the two integers are even
T If the two integers are even
then the sum of the integers is even

In order for a biconditional
statement to be true

Both the implication and its
converse must be true

If both are not true then
the statement is false

T An angle is a right angle
iff it measures 90°
T If the angle is a right angle
then it measures 90°
T If the angle measures 90°
then it is a right angle

True Biconditionals
are used as good definitions
in math.
They are given and accepted
as true

Valid Arguments
in Biconditionals

$$\begin{array}{l} P \leftrightarrow Q \\ Q \\ \hline \therefore P \end{array}$$

$$\begin{array}{l} P \leftrightarrow Q \\ \text{not } P \\ \hline \therefore \text{not } Q \end{array}$$