

# Chapter 7

## Logic and Proofs

We do Proofs at the End

Logic

## 7.1 Using and, or, and Not

And - compound event

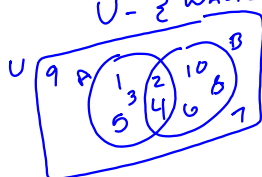
Or - Exclusive events

Not - Opposite  
Complimentary

$$A = \{1, 2, 3, 4, 5\}$$

$$B = \{2, 4, 6, 8, 10\}$$

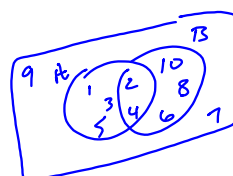
$$U = \{\text{Whole Numbers } 1-10\}$$



and - conjunction  
symbolically

$$A \cap B$$

In Both = 2, 4



Or - Disjunction

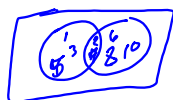
symbolically  
 $A \cup B$

Either  
 $\{1, 2, 3, 4, 5, 6, 8, 10\}$

Exclusive Or  $\oplus$

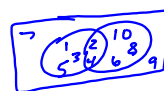
Say take out stuff they share

Either A or B but  
not both



$$\{1, 3, 5, 6, 8, 10\}$$

Not (Negation)



Not ( $A \cap B$ )  
Symbolically  
 $\sim \rightarrow$

$$\text{Not } A = \{6, 7, 8, 9, 10\}$$

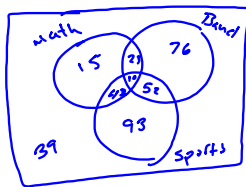
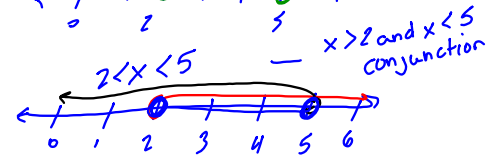
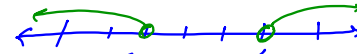
$$\{7, 9\}$$

If there are no elements that satisfy the set, there is still a set

Empty Set  
 $\{\emptyset\}$

or, and, not  
 in graphs

$x > 5$  or  $x < 2$  disjunction



If 350 people  
 39 not in  
 something

Math 90

$15 + 76 + 93$   
 $43 + 23 + 52$   
 10  
 311