

$$\begin{array}{r}
 5a + 2b = 23 \\
 + 7a - 2b = 13 \\
 \hline
 12a = 36
 \end{array}
 \quad
 \begin{array}{l}
 \frac{12a}{12} = \frac{36}{12} \\
 a = 3
 \end{array}$$

Need a new method

We can combine equations

$$\begin{array}{r}
 5(3) + 2b = 23 \\
 -15 \quad -15 \\
 \hline
 2b = 8 \\
 \frac{2b}{2} = \frac{8}{2} \\
 b = 4
 \end{array}
 \quad
 \begin{array}{l}
 (a, b) \\
 (3, 4)
 \end{array}$$

Adding / Subtracting
to solve systems

$$\begin{array}{r}
 3x - 4y = 10 \\
 + 2x + 4y = 5 \\
 \hline
 5x = 15 \\
 x = 3
 \end{array}
 \quad
 \begin{array}{r}
 3(3) - 4y = 10 \\
 -9 \quad -9 \\
 \hline
 -4y = 1 - \frac{1}{4} \\
 -4 \quad -4 \\
 4y = -1 \\
 y = -\frac{1}{4}
 \end{array}$$

(3, -1/4)

$$\begin{array}{r}
 2x + 3y = 5 \\
 + (2x + y = 3) \\
 \hline
 4x + 4y = 8
 \end{array}
 \quad
 \begin{array}{r}
 2x + 3y = 5 \\
 -2x - y = -3 \\
 \hline
 2y = 2 \\
 y = 1
 \end{array}$$

Sometimes we need to change
one of the equations

$$\begin{array}{r}
 2x + 1 = 3 \\
 2x = 2 \\
 x = 1
 \end{array}
 \quad
 (1, 1)$$

$$\begin{array}{r}
 4x + 2y = 5 \\
 2(3x - y = 5) \\
 \hline
 4(\frac{3}{2}) + 2y = 5
 \end{array}
 \quad
 \begin{array}{r}
 4x + 2y = 5 \\
 \frac{6x - 2y}{10x} = \frac{15}{8} \\
 x = \frac{15}{10} = \frac{3}{2}
 \end{array}$$

$$\begin{array}{r}
 6 + 2y = 5 \\
 -6 \quad -6 \\
 2y = -1 \\
 y = -\frac{1}{2}
 \end{array}
 \quad
 \left(\frac{3}{2}, -\frac{1}{2}\right)$$

We change
both to get rid
of one variable

$$\begin{array}{r}
 3(2x + 2y = 9) \\
 z(5x - 3y = -2) \\
 \hline
 6x + 6y = 27 \\
 10x - 6y = -4 \\
 \hline
 16x = 23
 \end{array}
 \quad
 \begin{array}{r}
 z(\frac{23}{16}) + 2y = 9 \\
 2(23) + 32y = 144 \\
 46 + 32y = 144 \\
 32y = 98 \\
 y = \frac{98}{32} = \frac{49}{16}
 \end{array}$$

$$\begin{array}{r}
 2x + 3y = 9 \\
 -2x - 3y = 18 \\
 \hline
 0 = 27
 \end{array}$$

Parallel lines
 don't work for.
 Linear combination

$$\begin{array}{r}
 2 - 14 \text{ even} \\
 \hline
 P & F \\
 \text{canned} & 8c & 3c \\
 \text{dry} & 6d & 1d \\
 \hline
 \overline{46} & & \overline{11}
 \end{array}$$