

## 7.1 Direct Variation, Slope and Tangent

### Direct Variation

$y$  varies directly with  $x$  if  $y = kx$  or  $\frac{y}{x} = k$   
where  $k$  is the variation constant

find  $k$  when  $y = 8$   $x = 2$   
then find  $y$  when  $x = \frac{3}{4}$

$$\begin{aligned} \rightarrow y &= kx & y &= k \cdot x \\ \frac{8}{2} &= \frac{k \cdot 2}{2} & y &= 4 \cdot \frac{3}{4} \\ 4 &= k & y &= \frac{4}{1} \cdot \frac{3}{4} = 3 \end{aligned}$$

find  $k$  when  $y = 4$   $x = 32$   
then find  $y$  when  $x = 96$

$$\begin{aligned} \frac{4}{32} &= \frac{k \cdot 32}{32} & y &= \frac{1}{8} \cdot 96 \\ \frac{1}{8} &= k & y &= 12 \end{aligned}$$

Slope  
rise  
run

$$\begin{array}{c} y = kx \\ \uparrow \\ \text{slope} \\ \downarrow \\ y = mx + b \end{array}$$

Slope Formula

$$\begin{aligned} m &= \frac{y_2 - y_1}{x_2 - x_1} & (2, 5) \\ & & (-3, 7) \\ m &= \frac{7 - 5}{-3 - 2} = \frac{2}{-5} = -\frac{2}{5} & (-10, 5) \\ & & (7, 12) \\ m &= \frac{12 - 5}{7 - (-10)} = \frac{7}{17} \end{aligned}$$

